GPU ACCELERATION OF ACOUSTIC FIELD PROPAGATOR

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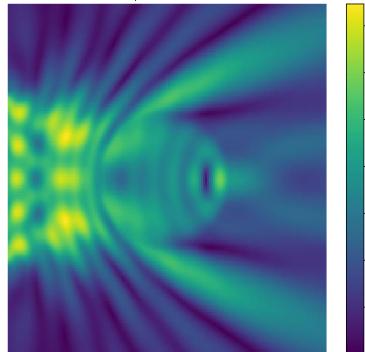


Motivation

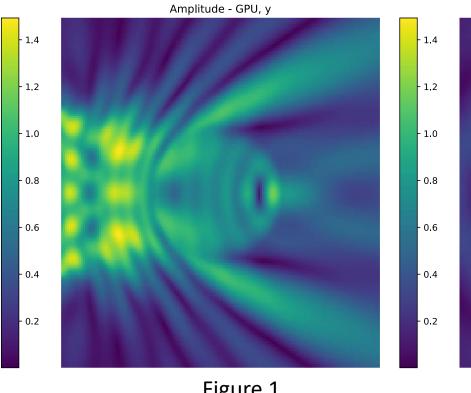
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Ultrasound simulation is needed to prevent accidental damage when used for transcranial ultrasound therapy.

Focus of this project is the speed-up of the original MATLAB implementation of Acoustic field propagator using GPU. Specifically, by using the CUDA toolkit.



Amplitude - GPU, x



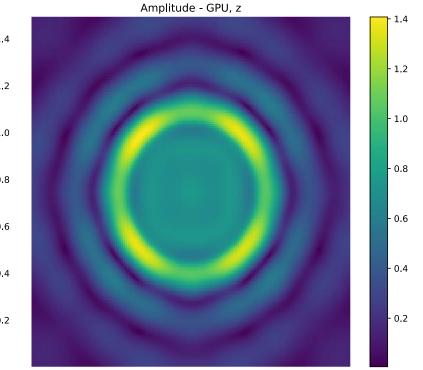


Figure 1

Acoustic field propagator

AFP computes the steady-state field pattern (complex pressure or amplitude and phase) from any phased array or acoustic source.

The method uses the Green's function for the homogeneous wave equation in k-space (spatial frequency domain)

The time convolution is solved analytically, and the remaining integrals are handled through a spatial Fourier transform. [Figure 2].

$$p(\mathbf{x}, t) = \mathcal{F}^{-1} \left\{ \mathcal{F} \left\{ A(\mathbf{x}) e^{i\phi(\mathbf{x})} \right\} I(\mathbf{k}, t) \right\}$$

Figure 2

$$I(\mathbf{k},t) = \left(\frac{e^{-\alpha c_0 t}}{c_0 \tilde{k}}\right) \frac{c_0 \tilde{k}(e^{(i\omega_0 + \alpha c_0)t} - \cos(c_0 \tilde{k}t)) - (i\omega_0 + \alpha c_0)\sin(c_0 \tilde{k}t)}{(c_0 k)^2 + 2i\alpha c_0\omega_0 - \omega_0^2}$$

This approach allows calculating the acoustic pressure across space for any time **t** > **0** in a single step without numerical integration.

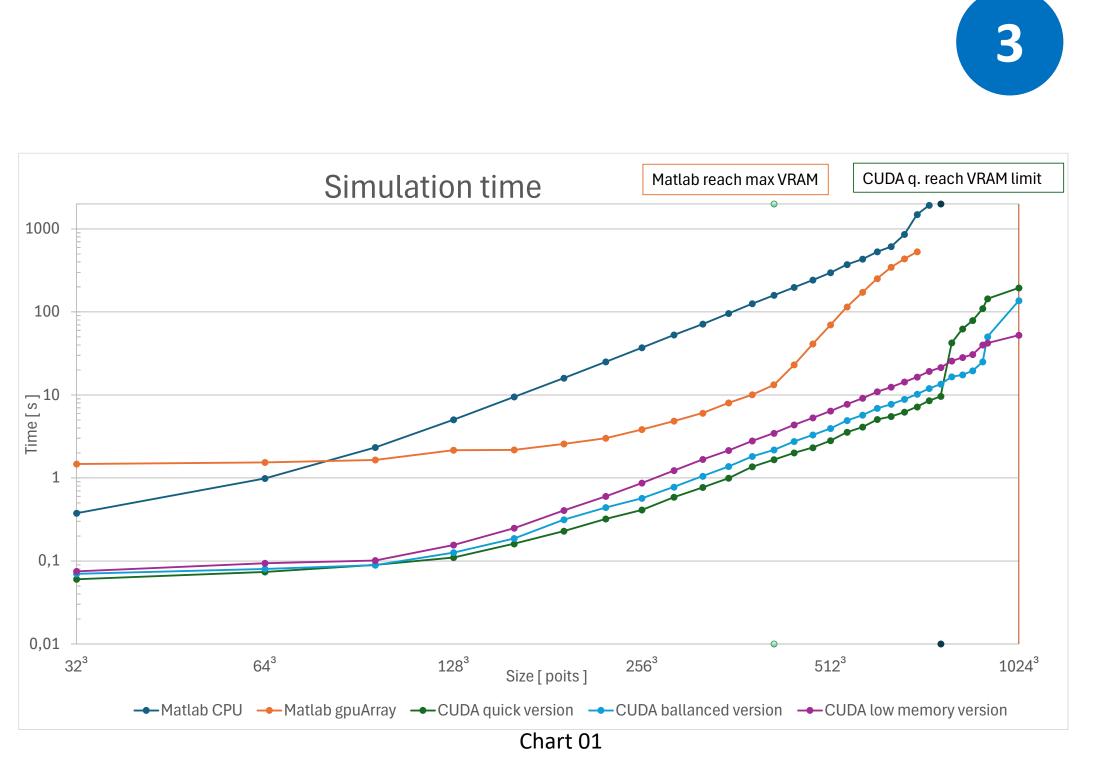
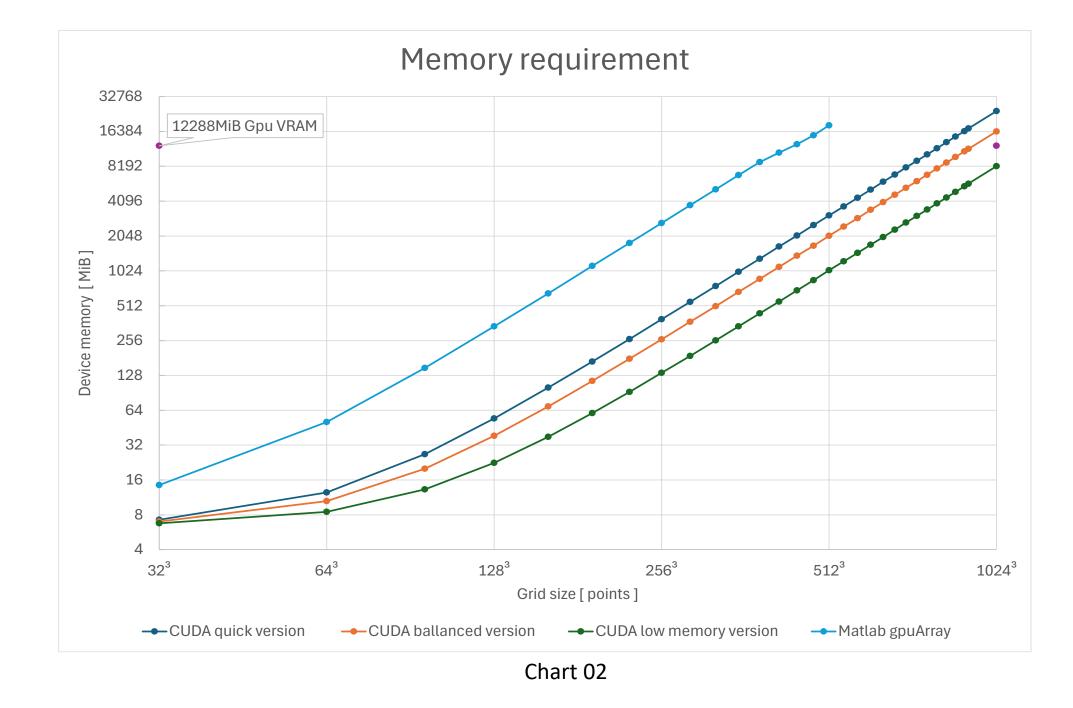


Figure 3

GPU acceleration

Project uses CUDA toolkit for the acceleration of the original MATLAB code on GPU.

- **Precomputed parts and variables** constant memory
- **Templated class with precision parameters**
- Use of CUDA graph for quicker kernel launching
- Reduction of memory transfers between GPU and system memory
- Multiple versions of AFP with different mem. requirements





In some cases, my version is up to 90 times quicker compared to the original version.

comparison with gpuArray Matlab version my In implementation is approximately 8 times quicker and uses 1/6 device memory.

User can fit even large acoustic grid with the use of low memory version that uses 1/3 of device memory, compared to quick version.

Tested on: CPU - Intel Core i7 13700k, RAM - DDR5 64 GB 5600 MHz GPU – Nvidia RTX 3080 Ti 12GB



This work was supported by the Ministry of Education, Youth and Sports of the Czech Republic through the e-INFRA CZ (ID:90254). This project has received funding from the European Unions Horizon Europe research and innovation programme under grant agreement No 101071008.