

1 Motivation

Ultrasound simulation is needed to prevent accidental damage when used for transcranial ultrasound therapy.

Focus of this project is the speed-up of the original MATLAB implementation of Acoustic field propagator using GPU. Specifically, by using the CUDA toolkit.

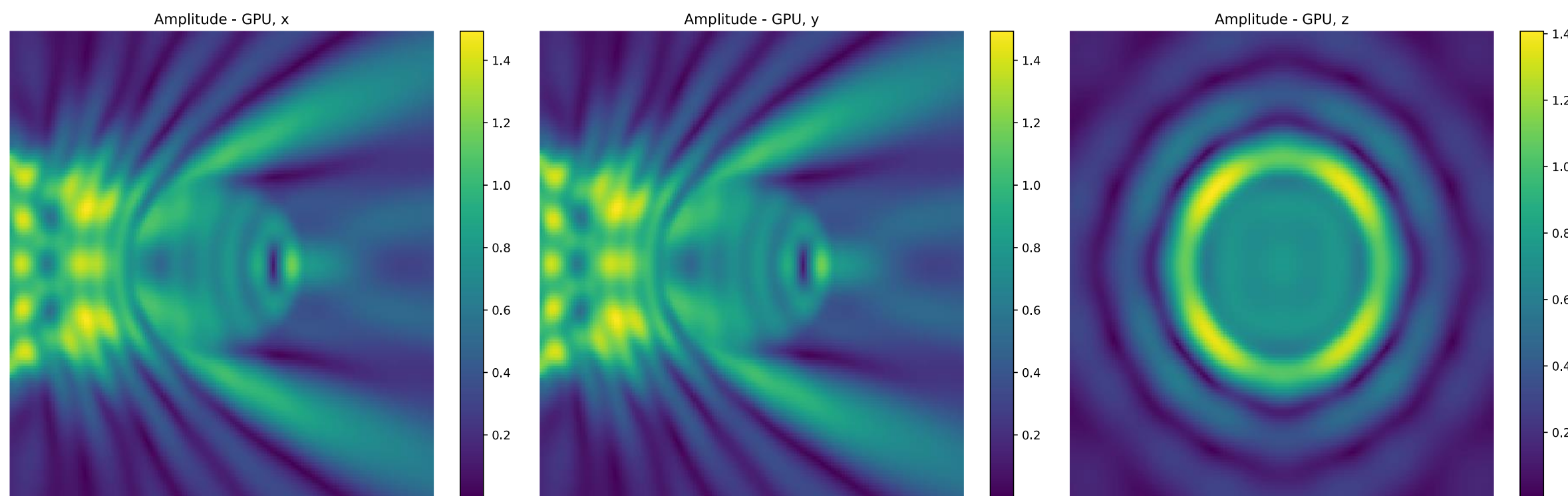


Figure 1

2 Acoustic field propagator

AFP computes the steady-state field pattern (complex pressure or amplitude and phase) from any phased array or acoustic source.

The method uses the Green's function for the homogeneous wave equation in k-space (spatial frequency domain)

The time convolution is solved analytically, and the remaining integrals are handled through a spatial Fourier transform. [Figure 2].

This approach allows calculating the acoustic pressure across space for any time $t > 0$ in a single step without numerical integration.

$$p(\mathbf{x}, t) = \mathcal{F}^{-1} \left\{ \mathcal{F} \left\{ A(\mathbf{x}) e^{i\phi(\mathbf{x})} \right\} I(\mathbf{k}, t) \right\}$$

Figure 2

$$I(\mathbf{k}, t) = \left(\frac{e^{-\alpha c_0 t}}{c_0 \tilde{k}} \right) \frac{c_0 \tilde{k} (e^{(i\omega_0 + \alpha c_0)t} - \cos(c_0 \tilde{k} t)) - (i\omega_0 + \alpha c_0) \sin(c_0 \tilde{k} t)}{(c_0 \tilde{k})^2 + 2i\alpha c_0 \omega_0 - \omega_0^2}$$

Figure 3

3

GPU acceleration

Project uses CUDA toolkit for the acceleration of the original MATLAB code on GPU.

- **Precomputed parts and variables** – constant memory
- **Templated class with precision parameters**
- **Use of CUDA graph for quicker kernel launching**
- **Reduction of memory transfers between GPU and system memory**
- **Multiple versions of AFP with different mem. requirements**

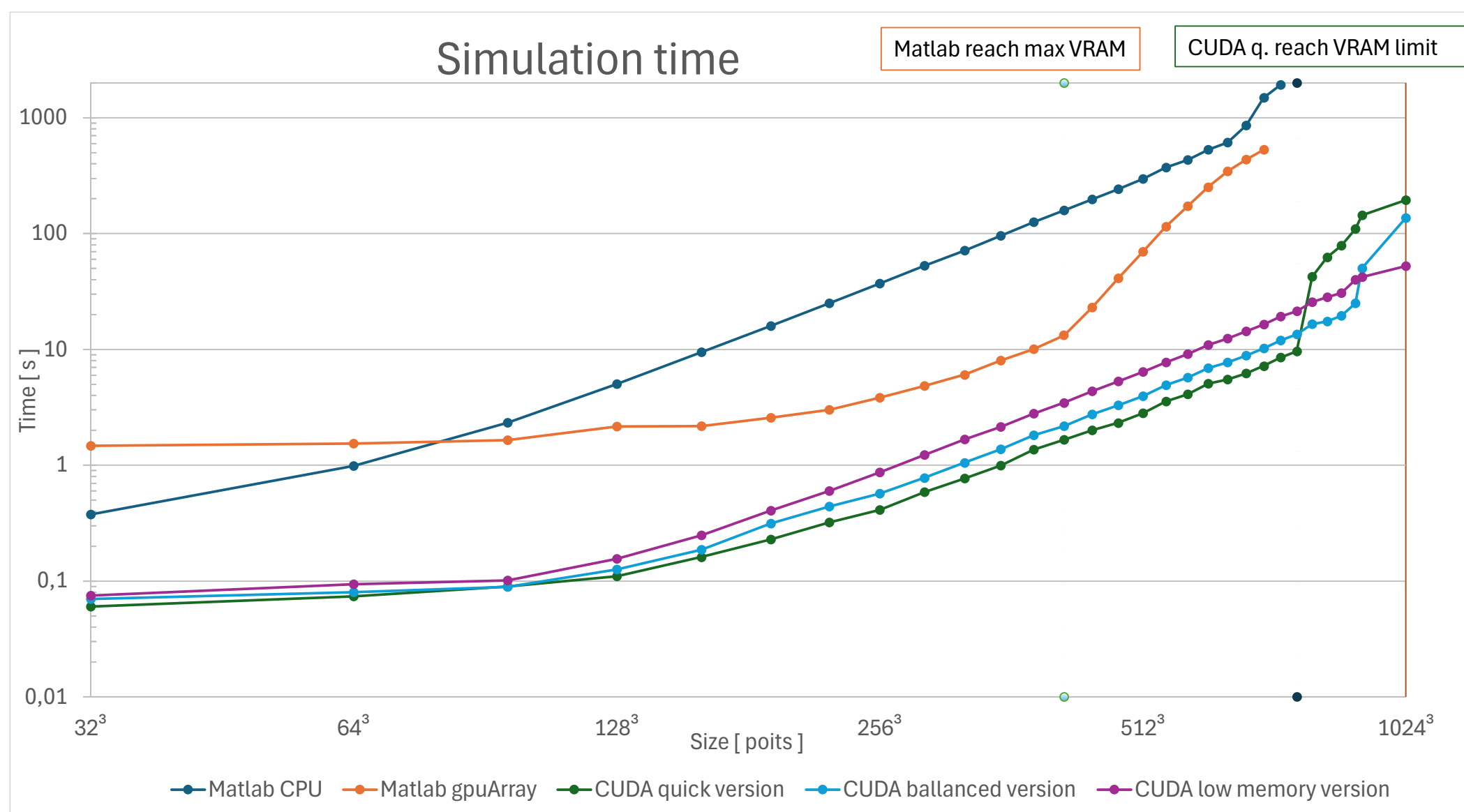


Chart 01

4

Result

In some cases, my version is up to 90 times quicker compared to the original version.

In comparison with gpuArray Matlab version my implementation is approximately 8 times quicker and uses 1/6 device memory.

User can fit even large acoustic grid with the use of low memory version that uses 1/3 of device memory, compared to quick version.

Tested on: CPU - Intel Core i7 13700k,
RAM - DDR5 64 GB 5600 MHz
GPU - Nvidia RTX 3080 Ti 12GB

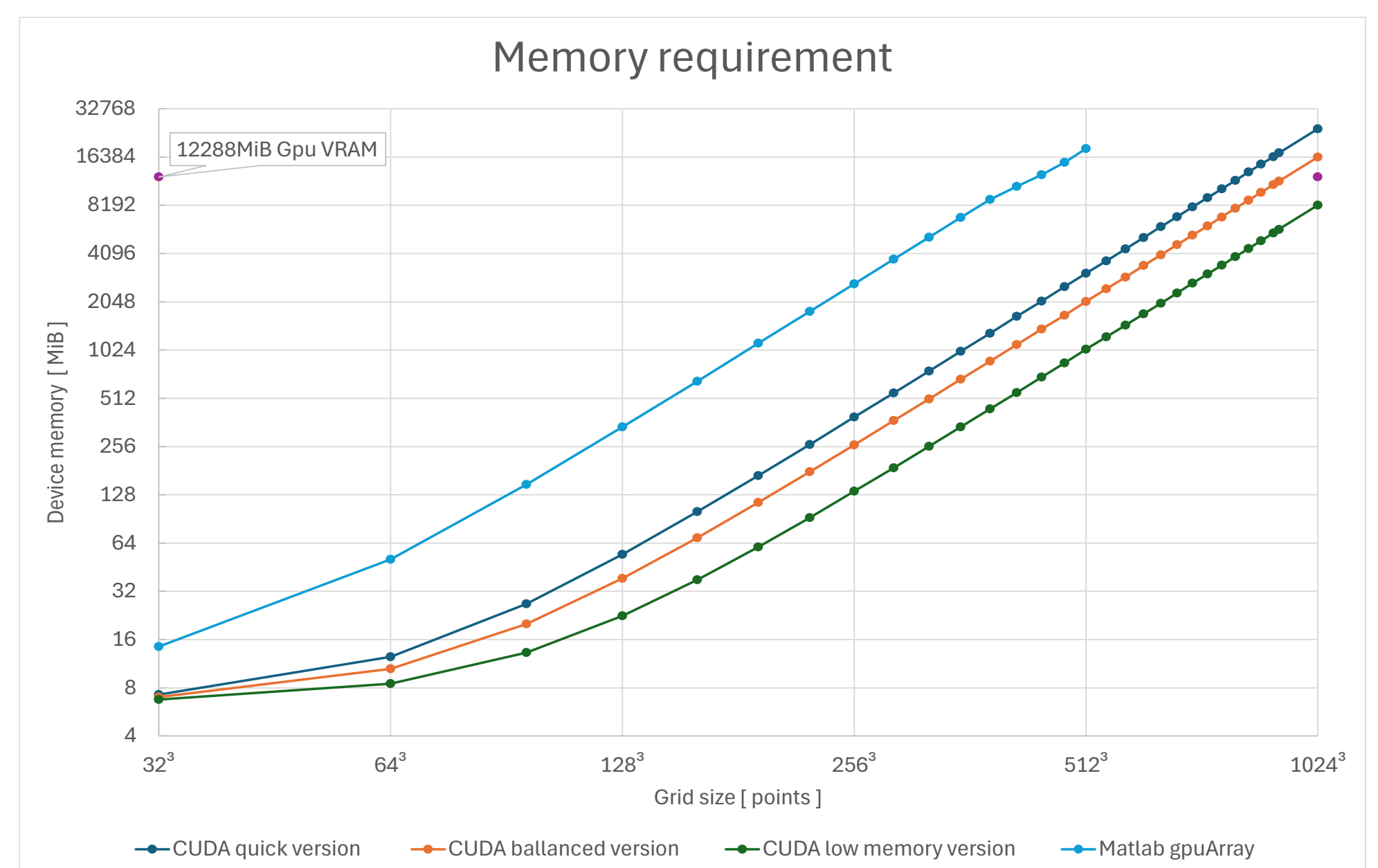


Chart 02